

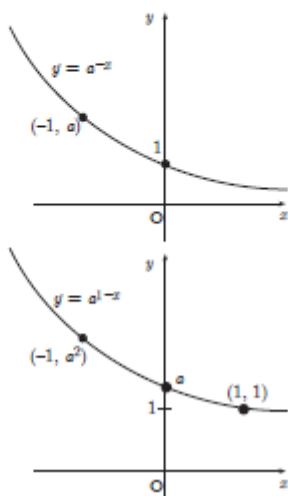
00 P1 B9	3B <ul style="list-style-type: none"> •¹ $\log_5 100 - \log_5 4$ •² $\log_5 25$ •³ 2
00 P2 B11	2A, 4A <ul style="list-style-type: none"> •¹ $m = \frac{1.8}{3} = 0.6$ •² $P = 0.6Q + 1.8$ •³ $\ln p = 0.6 \ln q + 1.8$ •⁴ $\ln q^{0.6}$ •⁵ $\ln 6 \cdot 05$ •⁶ $p = 6 \cdot 05 q^{0.6}$ •³ $\ln p = \ln a + b \ln q$ •⁴ $\ln p = 0.6 \ln q + 1.8$ •⁵ $\ln a = 1.8$ •⁶ $a = 6 \cdot 05, b = 0.6$ <p style="text-align: center;">OR</p>
01 P1 Q8	3C <ul style="list-style-type: none"> •¹ $\log_x 6^4 - \log_x 4^2$ •² $\log_x \frac{6^4}{4^2}$ •³ all processing leading to $x = 81$
01 P1 Q10	1B, 3A <ul style="list-style-type: none"> •¹ $a = 1$ and $b = 3$ •² a "log – shaped" graph of the same orientation •³ sketch passes through (0, –3) (labelled) •⁴ sketch passes through (7, 0) (labelled)
01 P2 Q9	3C <ul style="list-style-type: none"> •¹ $2A_0 = A_0 e^{k \times 1.5}$ •² e.g. $1.5k = \ln 2$ •³ $k = 0.46$
02 P1 Q11	4A <ul style="list-style-type: none"> •¹ $\log_5 y = -2(\log_5 x) + 1$ •² $\log_5 y = \log_5 x^{-2} + \dots$ •³ $\dots + \log_5 5$ •⁴ $y = 5x^{-2}$
02 P2 Q7	3B <ul style="list-style-type: none"> •¹ $\log_3(x-2) = -1$ •² $x-2 = 3^{-1}$ •³ $x = 2\frac{1}{3}$
2.(JA N) 02 P1	2B, 2A <ul style="list-style-type: none"> •¹ sketch with y – axis reflection •² sketch with translation f^1 to y – axis

	<ul style="list-style-type: none"> •³ (0, -7) •⁴ (-3, 0)
5.(JAN) 02 P1	<p>3A</p> <ul style="list-style-type: none"> •¹ $\log_a p + \log_a r = \cos^2 x + \sin^2 x$ •² $\log_a p + \log_a r = \log_a pr$ •³ $\log_a pr = 1$ and so $pr = a$ <p style="text-align: center;">OR</p> <ul style="list-style-type: none"> •¹ $p = a^{\cos^2 x} \quad r = a^{\sin^2 x}$ •² $pr = a^{\cos^2 x + \sin^2 x}$ •³ $pr = a^1 = a$
6.(JAN) 02 P2	<p>1C, 4B</p> <ul style="list-style-type: none"> •¹ 950 •² $9500 = 950 \times 2.6^{0.2t}$ •³ $\log_{10} 10 = \log_{10} 2.6^{0.2t}$ •⁴ $0.2t = \frac{\log_{10} 10}{\log_{10} 2.6}$ •⁵ $t \approx 12$ hours <p style="text-align: center;">OR $10 = 2.6^{0.2t}$</p>
03 P1 Q12	<p>4A</p> <ul style="list-style-type: none"> •¹ $\ln(2e)^3 - \ln(3e)^2$ •² $\ln\left(\frac{(2e)^3}{(3e)^2}\right)$ •³ $\ln\left(\frac{8e}{9}\right)$ •⁴ $1 + \ln(8) - \ln(9)$
03 P2 Q11	<div style="display: flex; align-items: center;"> <div style="flex: 1;"> <ul style="list-style-type: none"> •¹ expo sketch thr (0,2) •² expo sketch thr (0,a) •³ $a^{x+1} = a^x + 1$ •⁴ $a \times a^x - a^x = 1$ •⁵ $(a-1) \times a^x = 1 \dots \& \text{ complete}$ </div> <div style="flex: 1; text-align: center;"> </div> </div>

	<p style="text-align: center;">Alternative 1</p> <div style="border: 1px solid black; border-radius: 15px; padding: 10px; margin: 10px;"> <p style="text-align: center;"><i>Let</i> $x = \log_a\left(\frac{1}{a-1}\right)$</p> <p style="text-align: center;"><i>Then</i> $\frac{1}{a-1} = a^x$</p> <div style="display: flex; justify-content: space-around;"> <div> $y = a^x + 1$ $= \frac{1}{a-1} + 1$ $= \frac{a}{a-1}$ </div> <div> $y = a^{x+1}$ $= a^x \times a$ $= \frac{1}{a-1} \times a$ $= \frac{a}{a-1}$ </div> </div> <p>\therefore curves intersect at $\left(\log_a\left(\frac{1}{a-1}\right), \frac{a}{a-1}\right)$</p> </div> <div style="margin-left: 20px;"> <p style="text-align: center;">Alternative 2</p> <div style="border: 1px solid black; border-radius: 15px; padding: 10px; margin: 10px;"> <p style="text-align: center;"><i>Let</i> $x = \log_a\left(\frac{1}{a-1}\right)$</p> <p style="text-align: center;"><i>Then</i> $\frac{1}{a-1} = a^x$</p> <p style="text-align: center;">$1 = a^x(a-1)$</p> <p style="text-align: center;">$1 = a^{x+1} - a^x$</p> <p style="text-align: center;">$a^x + 1 = a^{x+1}$</p> <p>Hence the graphs intersect</p> </div> </div>
04 P1 Q9	<p>4A/B</p> <ul style="list-style-type: none"> •¹ $-\log_2 3^2$ •² $\log_2\left(\frac{x+1}{3^2}\right) = 3$ •³ $\frac{x+1}{3^2} = 2^3$ •⁴ $x = 71$ <p>OR</p> <ul style="list-style-type: none"> •¹ $\log_2(x+1) - 2\log_2 3 = 3\log_2 2$ •² $\log_2(x+1) = \log_2 2^3 + \log_2 3^2$ •³ $\log_2(x+1) = \log_2(2^3 \times 3^2)$ •⁴ $x = 71$
04 P2 Q10	<p>3C, 4A/B</p> <ul style="list-style-type: none"> •¹ $600 = A_0 e^{-0.002 \times 1000}$ •² $A_0 = \frac{600}{e^{-0.002 \times 1000}}$ •³ 4433 •⁴ $\frac{1}{2}A_0 = A_0 e^{-0.002t}$ •⁵ $0.5 = e^{-0.002t}$ •⁶ $-0.002t = \ln 0.5$ •⁷ $t = 347$ years <p>OR</p> <ul style="list-style-type: none"> •¹ $600 = A_0 e^{-0.002 \times 1000}$ •² $\ln A_0 = \ln 600 - \ln e^{-0.002 \times 1000}$ •³ $A_0 = 4433$
05 P1 Q7	2C, 1C

	<ul style="list-style-type: none"> •¹ $a = 4$ •² $b = 5$ •³ domain is $x > a$
05 P2 Q7	<p>4A</p> <div style="display: flex; justify-content: space-between;"> <div> <ul style="list-style-type: none"> •¹ $\log_4 \left(\frac{5-x}{3-x} \right)$ •² use $\log_a(b) = c \Leftrightarrow b = a^c$ •³ $\frac{5-x}{3-x} = 4^2$ •⁴ $x = \frac{43}{15}$ </div> <div> <ul style="list-style-type: none"> •¹ $\log_4 \left(\frac{5-x}{3-x} \right)$ •² $2 \log_4 4$ •³ $\left(\frac{5-x}{3-x} \right) = 4^2$ •⁴ $x = \frac{43}{15}$ </div> </div> <p style="text-align: center;">OR</p>
05 P2 Q9	<p>1B, 4A</p> <ul style="list-style-type: none"> •¹ $V_{t=0} = 252 \text{ (£m)}$ •² $252e^{-0.06335t} = 20$ •³ $e^{-0.06335t} = \frac{20}{252}$ •⁴ $-0.06335t = \ln\left(\frac{20}{252}\right)$ •⁵ $t = 40$
06 P1 Q10	<p>4A</p> <div style="display: flex; justify-content: space-between;"> <div> <ul style="list-style-type: none"> •¹ $\log_4(y) = \log_4(a^x)$ •² $3 = \log_4(a^6)$ •³ $a^6 = 4^3$ •⁴ $a = 2$ </div> <div> <ul style="list-style-type: none"> •³ $\log_4(a) = \frac{1}{2}$ •⁴ $a = 2$ </div> </div> <p style="text-align: center;">OR</p> <div style="display: flex; justify-content: space-between;"> <div> <ul style="list-style-type: none"> •¹ $\log_4(y) = mx + c$ •² $m = \frac{1}{2}, c = 0$ •³ $y = 4^{\frac{1}{2}x}$ •⁴ $y = \left(4^{\frac{1}{2}}\right)^x = 2^x \Rightarrow a = 2$ </div> <div> <ul style="list-style-type: none"> •¹ At A $\log_4(y) = 3$ •² $y = 4^3$ •³ $a^6 = 4^3$ •⁴ $a = 2$ </div> <div> <ul style="list-style-type: none"> •¹ $\log_4(y) = \log_4(a^x)$ •² $\log_4(y) = x \log_4(a)$ •³ $\log_4(a) = \frac{1}{2}$ •⁴ $a = 4^{\frac{1}{2}} = 2$ </div> </div> <p style="text-align: center;">OR</p>
06 P2 Q11	<p>5A/B</p> <ul style="list-style-type: none"> •¹ $A(t) = 0.88A_0$ stated or implied •² $e^{-0.000124t} = 0.88$ •³ $\ln\left(e^{-0.000124t}\right) = \ln(0.88)$ stated or implied •⁴ $-0.000124t = \ln(0.88)$ •⁵ $t = 1031$ years so claim valid <p style="text-align: center;">OR</p>

	<ul style="list-style-type: none"> •¹ $A(1000) = A_0 e^{-0.000124 \times 1000}$ •² $0.883A_0$ and 1000 year old piece of wood contains 88.3% carbon. •³ try a point where $t > 1030$ e.g. $A(1050)$ getting $0.878A_0$ •⁴ sketch of $y = A_0 e^{-0.000124t}$ showing <ul style="list-style-type: none"> 1. a monotonic decreasing function 2. points representing eg (1000, 88.3%) etc •⁵ observation that the point lies between the two plotted values for t and so claim valid.
07 P2 Q8	<p>4B</p> <ul style="list-style-type: none"> •¹ $\log_3(a - 1) - 2.2 = 0$ s/i by •² •² $\log_3(a - 1) = 2.2$ •³ $a - 1 = 3^{2.2}$ •⁴ $a = 12.2$ <p><i>Alt.method 1</i></p> <ul style="list-style-type: none"> •¹ $\log_3(a - 1) - 2.2 = 0$ s/i by •² •² $\log_3(a - 1) = 2.2$ •³ $\log_3(a - 1) = \log_3(11.21)$ •⁴ $a = 12.2$ <p><i>Alt.method 2</i></p> <ul style="list-style-type: none"> •¹ $\log_3(a - 1) - 2.2 = 0$ s/i by •² $\log_3(a - 1) - 2.2 \log_3 3 = 0$ •² $\log_3(a - 1) - \log_3(11.21) = 0$ •³ $\log_3 \frac{(a-1)}{11.21} = 0$ •⁴ $a = 12.2$
07 P2 Q9	2B, 2A



	<ul style="list-style-type: none"> •¹ reflecting in y-axis and passing thr' e.g. $(0,1)$ •² passing thr' 1 more point e.g. $(-1,a)$ or $\left(1, \frac{1}{a}\right)$ •³ vertical scaling of "a" and passing thr' e.g. $(0,a)$ •⁴ passing thr' 1 more point e.g. $(-1,a^2)$ or $(1,1)$ 
07 P2 Q11	1B, 1C, 4A <ul style="list-style-type: none"> •¹ $a = \frac{1}{2}$ •² $b = \frac{3}{2}$ •³ $\log_{10}(y) = \log_{10}(3 \times 4^x)$ •⁴ $\log_{10}(y) = \log_{10}(3) + \log_{10}(4^x)$ •⁵ $\log_{10}(y) = x \log_{10}(4) + \log_{10}(3)$ •⁶ gradient = $\log_{10}(4)$ or equivalent <div style="display: flex; justify-content: space-between;"> <div></div> <div> Alternative Method <ul style="list-style-type: none"> •¹ $y = 10^{Px+Q}$ •² $y = 10^Q \times (10^P)^x$ •³ $10^Q = 3$ and $10^P = 4$ •⁴ $P = \log_{10} 4$ </div> </div>
08 P1 Q23	3C, 5A/B <ul style="list-style-type: none"> •¹ $h(f(x)) = h(x^2 - x + 10)$ s / i by •² •² $\log_2(x^2 - x + 10)$ •³ $\log_2(5 - x)$ •⁴ $\log_2\left(\frac{x^2 - x + 10}{5 - x}\right)$ •⁵ $\frac{x^2 - x + 10}{5 - x} = 2^3$ •⁶ $x^2 - x + 10 = 8(5 - x)$ •⁷ $x^2 + 7x - 30 = 0$ •⁸ $x = 3, -10$
09 P2 Q3	4C, 5B

	<div> $\begin{array}{r rrrr} & 1 & 8 & 11 & -20 \\ 1 & 1 & & & \\ \hline & 1 & 9 & & \\ & 1 & 8 & 11 & -20 \\ 1 & 1 & 9 & 20 & \end{array}$ </div> <div> $\begin{array}{r rrrr} & 1 & 8 & 11 & -20 \\ 1 & 1 & 9 & 20 & \end{array}$ </div> <div> $rem. = 0$ </div> <div> $so\ x = 1\ is\ root$ </div> <div> OR </div> <div> $f(1) = 1 + 8 + 11 - 20 = 0\ so\ x = 1\ is\ a\ root$ </div> <div> $(x - 1)(x^2 + 9x + 20)$ </div> <div> $(x - 1)(x + 4)(x + 5)$ </div> <div> $\log_2((x + 3)(x^2 + 5x - 4))$ </div> <div> $(x + 3)(x^2 + 5x - 4) = 2^3$ </div> <div> $x^3 + 8x^2 + 11x - 20 = 0$ </div> <div> $x = 1\ or\ x = -4\ or\ x = -5$ </div> <div> $x = 1\ only$ </div> <div> <p>Stated explicitly</p> </div> <div> <p>s / l by</p> </div> <div> <p>Stated explicitly here</p> </div>
09 P2 Q6	<div> <p>2B, 3A</p> </div> <div> $61e^{0.016 \times 14}$ </div> <div> $76\ million\ or\ equiv.$ </div> <div> $10.2 = 5.1e^{0.0043t}$ </div> <div> $0.0043t = \ln 2$ </div> <div> $t = 161.2\ years$ </div> <div> <p>Options</p> </div> <div> <p>1</p> </div> <div> $61000000e^{0.016 \times 14}$ </div> <div> 76000000 </div>
10 P2 Q7	<div> <p>convert from log to exponential form know to and convert back to log form process and complete</p> </div> <div> $x = 4^p$ </div> <div> $\log_{16} x = \log_{16} 4^p$ </div> <div> $\log_{16} x = p \times \log_{16} 4\ and\ complete$ </div> <div> $\log_3 x + \frac{1}{2} \log_3 x = 12$ </div> <div> $\log_3 x = 8$ </div> <div> $x = 3^8\ (= 6561)$ </div> <div> <p>or</p> </div> <div> $Q + \frac{1}{2}Q = 12$ </div> <div> $Q = 8$ </div> <div> $\log_3 x = 8$ </div> <div> $x = 3^8\ (= 6561)$ </div> <div> $2\log_9 x + \log_9 x = 12$ </div> <div> $\log_9 x = 4$ </div> <div> $x = 9^4\ (= 6561)$ </div> <div> <p>or</p> </div> <div> $2Q + Q = 12$ </div> <div> $Q = 4$ </div> <div> $\log_9 x = 4$ </div> <div> $x = 9^4\ (= 6561)$ </div>

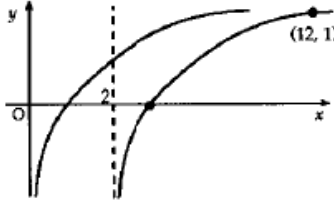
11 P2 Q5	introduce logarithms to $y =$ use laws of logarithms interpret intercept solve for k interpret gradient	Method 1 <ul style="list-style-type: none">•¹ $\log_2 y = \log_2 kx^n$•² $\log_2 y = n \log_2 x + \log_2 k$•³ $\log_2 k = 5$ or $\log_2 y = 5$•⁴ $k = 32$ or 2^5•⁵ $n = \frac{1}{2}$ Method 2 <ul style="list-style-type: none">•¹ $\log_2 y = \frac{1}{2} \log_2 x + 5$•² $\dots + 5 \log_2 2$ or $\dots + \log_2 2^5$•³ $\log_2 y = \log_2 x^{\frac{1}{2}} + \dots$•⁴ $\log_2 y = \log_2 2^5 x^{\frac{1}{2}}$•⁵ $y = 2^5 x^{\frac{1}{2}}$	stated explicitly stated explicitly Accept without working Accept without working
12 P2 Q7	equate expressions for y take logarithms of both sides use law of logs : $\log_a x^n = n \log_a x$ gather like terms use law of logs : $\log_a p + \log_a q = \log_a pq$ complete to required form substitute in for x process y Method 2 <ul style="list-style-type: none">•¹ $4^x = 3^{2-x}$•² $\log_3(4^x) = 2 - x$•³ $x \log_3 4 = 2 - x$•⁴ $x = \frac{2}{1 + \log_3 4}$•⁵ $\frac{2 \log_3 3}{\log_3 12}$	<ul style="list-style-type: none">•¹ $4^x = 3^{2-x}$•² $\log_a(4^x) = \log_a(3^{2-x})$•³ $x \log_a 4 = (2 - x) \log_a 3$•⁴ $x(\log_a 4 + \log_a 3) = 2 \log_a 3$•⁵ $x \log_a 12 = \log_a 9$•⁶ $\frac{\log_a 9}{\log_a 12}$•⁷ e.g. $y = 4^{\frac{\log_a 9}{\log_a 12}}$•⁸ e.g. $y \approx 4^{0.8842} \approx 3.4$ Method 3 <ul style="list-style-type: none">•¹ $4^x = 3^{2-x}$•² $4^x = \frac{3^2}{3^x}$•³ $12^x = 9$•⁴ $\log_a 12^x = \log_a 9$•⁵ $x \log_a 12 = \log_a 9$	stated, or implied stated explicitly

13 P2 Q5	<p>use correct law of logs</p> <p>know to and convert to exponential form</p> <p>express as an equation in standard quadratic form</p> <p>solve quadratic</p>	<p>•¹ $\log_5 [(3 - 2x)(2 + x)] = 1$ stated or implied by •²</p> <p>•² $(3 - 2x)(2 + x) = 5^1$</p> <p>•³ $2x^2 + x - 1 = 0$</p> <p>•⁴ $x = \frac{1}{2}, x = -1$</p>
13 P2 Q9	<p>interpret half-life</p> <p>process equation</p> <p>write in logarithmic form</p> <p>process for k</p> <p>interpret equation</p> <p>process</p> <p>state percentage decrease</p>	<p>•¹ $\frac{1}{2} P_0 = P_0 e^{-25k}$ stated or implied by •²</p> <p>•² $e^{-25k} = \frac{1}{2}$</p> <p>•³ $\log_e \frac{1}{2} = -25k$</p> <p>•⁴ $k \approx 0.028$</p> <p>•⁵ $P_t = P_0 e^{-80 \times 0.028}$</p> <p>•⁶ $P_t \approx 0.1065 P_0$</p> <p>•⁷ 89%</p>
14 P1 Q24	<p>take \log_9 of both sides of the equation</p> <p>apply laws of logarithms</p> <p>apply laws of logarithms</p> <p>find k</p> <p>find a</p> <p>know to use equation of the line</p> <p>write in exponential form</p> <p>apply laws of indices</p> <p>find k</p> <p>find a</p>	<p>Method 1</p> <p>•¹ $\log_9 y = \log_9 ka^x$</p> <p>•² $\log_9 y = \log_9 k + \log_9 a^x$</p> <p>•³ $\log_9 y = \log_9 k + x \log_9 a$</p> <p>•⁴ $\log_9 k = 2, k = 81$ or $k = 9^2 = 81$</p> <p>•⁵ $\log_9 a = \frac{1}{2}, a = 3$ or $a = 9^{\frac{1}{2}} = 3$</p> <p>Method 2</p> <p>•¹ $\log_9 y = \frac{1}{2}x + 2$</p> <p>•² $y = 9^{\frac{1}{2}x + 2}$</p> <p>•³ $y = 9^{\frac{1}{2}x} 9^2$</p> <p>•⁴ $k = 81$</p> <p>•⁵ $a = 3$</p>

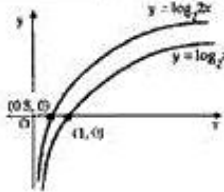
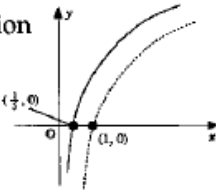
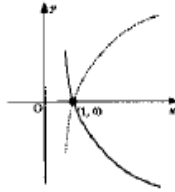
ANSWERS - Pre 2000 - Exponential Graphs

1	<ul style="list-style-type: none"> •¹ $t = a$ •² $u = 0$ •³ both passing thr' same point on y-axis •⁴ $y = a^{2x}$ starting below $y = a^x$ and finishing above •⁵ $(1, a^2)$ 	 <p>For mark 3</p>  <p>For mark 4</p>
2	<ul style="list-style-type: none"> •¹ $3 = ke^0 \Rightarrow k = 3$ •² $y = 3e^{0.5}$ or equivalent •³ $(1, 4.9)$ 	

ANSWERS - Pre 2000 - Log Graphs

1	<ul style="list-style-type: none"> •¹ know $x = 2$ is asymptote •² graph passes thr' $(3, 0)$ •³ graph passes thr' another marked point e.g. $(12, 1)$ 	
2	<ul style="list-style-type: none"> •¹ $\log_{10}(-2 + a) = 0$ •² 3 	
3	<ul style="list-style-type: none"> •¹ $a = -2$ •² $1 = \log_b(7 - 2)$ •³ $b = 5$ 	<p>OR</p> <ul style="list-style-type: none"> •¹ $1 = \log_b(7 + a)$ and $0 = \log_b(a + 3)$ •² $7 + a = b$ and $a + 3 = b^0$ •³ $a = -2, b = 5$

ANSWERS - Pre 2000 - Log Graphs using Laws of Logs

1	<ul style="list-style-type: none"> •¹ strat: $\log_2 2x = \log_2 2 + \log_2 x$ •² translating graph upwards 1 unit •³ $(\frac{1}{2}, 0)$ clearly marked 	
2	<ul style="list-style-type: none"> •¹ sketch of new function •² $\log_5 x + 1 = 0$ •³ $(\frac{1}{5}, 0)$ 	<ul style="list-style-type: none"> •⁴ $\log_5 \frac{1}{x} = -\log_5 x$ •⁵ reflect in x-axis 
3	<ul style="list-style-type: none"> •¹ $b = 2$ •² $3 = a \log_2 2$ stated or implied or $(4 - b)^a = 8$ •³ $a = 3$ 	

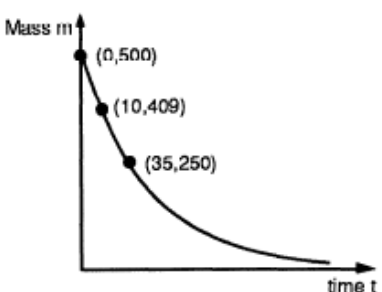
4	<ul style="list-style-type: none"> •¹ $x_A = -4 \cdot 5$ •² $5 \log_{10}(2x + 10) = 8$ •³ $2x + 10 = 10^{\frac{8}{5}}$ •⁴ $x = 14 \cdot 9$
5	<p>(a)</p> <ul style="list-style-type: none"> •¹ graph of $y = 2 - x$ with two annotated points eg (2,0) and (0,2) •² graph of $y = \log_{10} x$ with one annotated point eg (1,0) •³ any consistent approximation <p>(b)</p> <ul style="list-style-type: none"> •⁴ between 1.7 and 1.8 •⁵ between 1.75 and 1.80 •⁶ 1.76

ANSWERS - Pre 2000 - Log Equations

1	<ul style="list-style-type: none"> •¹ $6 \cdot 5 = 10 \log_{10} \left(\frac{P}{30} \right)$ •² $P = 30 \times 10^{0.65}$ •³ 134 phons
2	<ul style="list-style-type: none"> •¹ $x = \log_5 12$ •² $5^x = 12$ •³ $\log 5^x = \log 12$ •⁴ $\frac{\log_{10} 12}{\log_{10} 5}$ or $\frac{\log_e 12}{\log_e 5}$ or $\frac{\log 12}{\log 5} = 1.54$
3	<ul style="list-style-type: none"> •¹ $k = \log_e p$ and $k = \frac{1}{2} \log_e q$ •² $\log p = \frac{1}{2} \log q$ or $p = e^k$ and $q = e^{2k}$ •³ $q = p^2$ or $p = q^{\frac{1}{2}}$ •⁴ $q = 25$

ANSWERS - Pre 2000 - Exponential Equations

1	<ul style="list-style-type: none"> •¹ use logs •² $\ln 3^x = \ln 42$ •³ $x \ln 3 = \ln 42$ •⁴ 3.402 	OR	<ul style="list-style-type: none"> •¹ use logs •² $x = \log_3 42$ •³ $x = \frac{\ln 42}{\ln 3}$ •⁴ 3.402 	OR	<ul style="list-style-type: none"> •¹ use exponentials •² $(e^{1.0986})^x = 42$ •³ $1.0986x = \ln 42$ •⁴ 3.402
2	<ul style="list-style-type: none"> •¹ 40 •² $40e^{1.5t} = 80$ •³ $1.5t = \ln 2$ •⁴ $t = 0.46$ •⁵ 28 minutes 				

3	<ul style="list-style-type: none"> •¹ $75 = 100e^{-k \times 15}$ •² $\ln 0.75 = -15k$ •³ $k = 0.0192$ •⁴ $T_{15} = 75e^{-0.0192 \times 15}$ or $T_{30} = 100e^{-0.0192 \times 30}$ •⁵ fall = 18.75
4	<ul style="list-style-type: none"> •¹ $9 = 10e^{-3k}$ •² $-3k = \log_e 0.9$ •³ 0.04 •⁴ $e^{-kt} = 0.5$ •⁵ a correct value for t
5	<p>(a)</p> <ul style="list-style-type: none"> •¹ $m = 500e^{-0.02 \times 10}$ •² 409.37 grams <p>(b)</p> <ul style="list-style-type: none"> •³ $250 = 500e^{-0.02t}$ •⁴ $\ln 250 = \ln 500 - 0.02t \times 1$ or equiv. •⁵ 34.7 years <p>(c)</p> <ul style="list-style-type: none"> •⁶ any two of the 3 points •⁷ the remaining point •⁸ a decreasing curve 
6	<ul style="list-style-type: none"> •¹ $(0, 5) \Rightarrow a = 5$ •² $20 = 5e^{3k}$ •³ e.g. $\ln 20 = \ln 5 + 3k \ln e$ •⁴ $k = 0.462$ (Accept $\frac{1}{3} \ln 4$) •⁵ $y = 5e^{k(x-3)}$
7	<p>(a)</p> <ul style="list-style-type: none"> •¹ $10 = 50e^{-24k}$ •² $0.2 = e^{-24k}$ •³ $-24k = \ln 0.2$ •⁴ $-24k = -1.609$ •⁵ $k = 0.067$ <p>(b)</p> <ul style="list-style-type: none"> •⁶ knowing to find P_4 •⁷ $P_4 = 50e^{-0.067 \times 4}$ •⁸ 38 •⁹ $38 > 30$ so can be driven further

8	<p>(a)</p> <ul style="list-style-type: none"> •¹ $\frac{1}{2}y_0 = y_0 e^{5700k}$ •² $\ln \frac{1}{2} = 5700k$ •³ $k = -0.000122$ <p>(b)</p> <ul style="list-style-type: none"> •⁴ $y = y_0 e^{-0.000122 \times 1000}$ •⁵ $\frac{y}{y_0} = \dots$ •⁶ 88.5%
9	<p>(a)</p> <ul style="list-style-type: none"> •¹ $90 = 120e^{-4k}$ •² $e^{-4k} = 0.75$ <i>or</i> $\ln 90 = \ln 120 + \ln e^{-4k}$ •³ $\ln 0.75 = -4k$ •⁴ $k = 0.0719$ <p>(b)</p> <ul style="list-style-type: none"> •⁵ $I_{10} = I_0 e^{-10 \times 0.0719}$ <i>stated or implied by</i> •⁶ •⁶ $\frac{I_{10}}{I_0} = 0.487$ •⁷ 51.3% reduction

ANSWERS - Pre 2000 - Graphs with Log Axes

1	<ul style="list-style-type: none"> •¹ <i>use</i> $y = mx + c$ •² $\log_{10} y = 2 \log_{10} x + 1$ •³ $\log_{10} y = 2 \log_{10} x + \log_{10} 10$ •⁴ $\log_{10} y = \log_{10} x^2 + 1$ •⁵ $\log_{10} y = \log_{10} 10x^2$ •⁶ $y = 10x^2$
2	<p>(a)</p> <ul style="list-style-type: none"> •¹ $\log_e y = \log_e a e^{bx}$ •² $\log_e y = \log_e a + \log_e e^{bx}$ •³ $\log_e y = \log_e a + bx$ <p>(b)</p> <ul style="list-style-type: none"> •⁴ evidence for strategy being carried out will be appearance of two equations at •⁵ stage •⁵ e.g. $3.1b + \log a = 9.99$, $5.2b + \log a = 16.29$ •⁶ strategy: know to subtract •⁷ $b = 3$ •⁸ $a = e^{0.69}$ •⁹ $a = 2$

3	<p>(a)</p> <ul style="list-style-type: none"> •¹ $e.g. m = 3$ •² $e.g. 8.70 = 3 \times 2.65 + c$ or <i>equiv.</i> •³ $e.g. Y = 3X + 0.75$ <p>(b)</p> <ul style="list-style-type: none"> •⁴ $\ln y = 3 \ln x + 0.7$ •⁵ $\ln y = \ln 2.01x^3$ •⁶ $b = 3$ •⁷ $a = 2.01$
4	<p>(a)</p> <ul style="list-style-type: none"> •¹ $m = -\frac{4}{5}$ stated or implied •² $y = mx + 4$ stated or implied •³ $\log_e I = -\frac{4}{5} \log_e t + 4$ <p>(b)</p> <ul style="list-style-type: none"> •⁴ $\log_e t^{-\frac{4}{5}}$ •⁵ $\log_e 54.6$ •⁶ $\log_e 54.6t^{-\frac{4}{5}}$ •⁷ $I = 54.6t^{-0.8}$